

## SZLZ107 - Criteria of starting in fatigue under multiaxial loadings for a localization criticizes structure

### Summary:

The purpose of this test is the multiaxial calculation of the criteria of tiredness for the periodic loadings and not-periodicals while using `POST_FATIGUE` for a localization structure criticizes. The objective of this CAS-test is to find same the computation results got by `CALC_FATIGUE`.

modeling A	criteria <code>CROSSLAND</code> , <code>DANG VAN-PAPADOPOULOS</code> and in formula
modeling B	criteria in formulas (to find the results of CAS-test <code>SSLV135D</code> ), <code>'MATAKE_MODI_AC'</code> , <code>DANG_VAN_MODI_AC</code> (to find the results of CAS-tests <code>SSLV135With</code> );
modeling C	criteria in formulas (to find the results of CAS-test <code>SSLV135E</code> );
modeling D	criteria in formulas (to find the results of CAS-test <code>SSLV135F</code> );
modeling E	criteria in formulas, <code>'MATAKE_MODI_AV'</code> , <code>DANG_VAN_MODI_AV</code> , <code>FATESOCI_MODI_AV</code> (to find the results of CAS-tests <code>SSLV135B</code> )
modeling F	criteria <code>MATAKE_MODI_AC</code> , <code>DANG_VAN_MODI_AC</code> , <code>MATAKE_MODI_AV</code> , <code>DANG_VAN_MODI_AV</code> , <code>FATESOCI_MODI_AV</code> . One tests the change of the direction of the critical plan on which the damage or shearing is maximum
modeling G	criteria in formulas of the standard plan criticizes with keyword <code>FORMULE_CRITIQUE</code> (to find the results of CAS-tests <code>SSLV135H</code> and <code>SSLV135A</code> );

Results provided by the operator `POST_FATIGUE` are completely satisfactory.

## 1 Problem of reference

### 1.1 Modeling A

The analysis consists in determining the criterion of CROSSLAND and the criterion of DANG VAN - PAPADOPOULOS in a point of a structure subjected to a radial periodic multiaxial loading.

**Criterion of CROSSLAND:**

$$\tau_a + a P_{max} - b \leq 0 \text{ where:}$$

$$\tau_a = \frac{1}{2} \text{Max}_{0 \leq t_0 \leq T} \text{Max}_{0 \leq t_1 \leq T} \|\tilde{s}(t_1) - \tilde{s}(t_0)\| = \frac{1}{2} \text{Max}_{0 \leq t_0 \leq T} \text{Max}_{0 \leq t_1 \leq T} \sqrt{\frac{1}{2}(\tilde{s}_{11}^2 + \tilde{s}_{22}^2 + \tilde{s}_{33}^2 + 2\tilde{s}_{12}^2 + 2\tilde{s}_{13}^2 + 2\tilde{s}_{23}^2)}$$

amplitude de scission

avec  $\tilde{s}$  déviateur du tenseur des contraintes  $\sigma$

$$P_{max} = \text{Max}_{0 \leq t \leq T} \left( \frac{1}{3} \text{trace}(\sigma) \right) = \text{maximum hydrostatic pressure}$$

$$a = \left( \tau_0 - \frac{d_0}{\sqrt{3}} \right) / \frac{d_0}{3} \text{ and } b = \tau_0$$

with  $\tau_0$  = limit of endurance in alternate pure shearing

$d_0$  = limit of endurance in alternate pure traction and compression

The criterion is:  $R_{crit} = \tau_a + a P_{max} - b$

If  $R_{crit}$  is negative or null, there is no damage. If  $R_{crit}$  is positive, it is likely to have damage there.

**Criterion of DANG VAN-PAPADOPOULOS:**

$$K^* + a P_{max} - b \leq 0$$

where  $K^* = R / \sqrt{2}$  where  $R$  ray of the smallest sphere circumscribed with the way of loading within the space of diverters of constraints  $\tilde{s}$ .

$$R = \text{Max}_{0 \leq t \leq T} \sqrt{(\tilde{s}(t) - C^*) : (\tilde{s}(t) - C^*)} \text{ where } C^* \text{ is the center of the hypersphère}$$

$$C^* = \text{Min}_{C \in K} \text{Max}_{0 \leq t \leq T} \sqrt{(\tilde{s}(t) - C) : (\tilde{s}(t) - C)}$$

$$P_{max} = \text{Max}_{0 \leq t \leq T} \left( \frac{1}{3} \text{trace}(\sigma) \right) = \text{maximum hydrostatic pressure}$$

$$a = \left( \tau_0 - \frac{d_0}{\sqrt{3}} \right) / \left( \frac{d_0}{3} \right) \text{ and } b = \tau_0$$

with  $\tau_0$  = limit of endurance in alternate pure shearing

$d_0$  = limit of endurance in alternate pure traction and compression

The criterion is:  $R_{crit} = K^* + a P_{max} - b$

If  $R_{crit}$  is negative or null, there is no damage. If  $R_{crit}$  is positive, it is likely to have damage there.

## 1.1.1 Material properties

$\tau_0$  = limit of endurance in alternate pure shearing = 352. MPa

$d_0$  = limit of endurance in alternate pure traction and compression = 540.97 MPa

## 1.1.2 History of the loading

$t$	1.	2.	3.
$\sigma_{xx}(t)$	411.	0.	- 411.
$\sigma_{xy}(t)$	205.	0.	- 205.
$\sigma_{yy}(t) = \sigma_{zz}(t) = \sigma_{xz}(t) = \sigma_{yz}(t)$	0.	0.	0.

The loading is considered periodic.

## 1.2 Modeling B

The material properties and the history of loading identical and are obtained starting from CAS-tests SSLV135A.

## 1.3 Modeling C

The material properties and the history of loading identical and are obtained starting from CAS-test SSLV135E .

## 1.4 Modeling D

The material properties and the history of loading identical and are obtained starting from CAS-test SSLV135F .

## 1.5 Modeling E

Properties of materials and the history of loading identical and are obtained starting from CAS-test SSLV135B .

## 1.6 Modeling F

Properties of materials and the history of loading identical and are obtained starting from the cases test SSLV135G

## 1.7 Modeling G

Properties of materials and the history of loading identical and are obtained starting from the cases test SSLV135H and SSLV135With

## 2 Reference solution

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### 2.1 Modeling A

#### 2.1.1 Method of calculating used for the reference solution

The results of reference result from the thesis of I. PAPADOPOULOS [bib1]. For the criterion of **CROSSLAND**, one can also obtain them manually.

The loading being radial the two criteria must provide the same results.

#### 2.1.2 Results of Reference

For **criterion of CROSSLAND**, the value of the amplitude of scission, the value of the maximum hydrostatic pressure and the value of the criterion are tested:

$$\tau_a = 313.579 \text{ Mpa} \quad P_{max} = 137. \text{ Mpa} \quad R_{crit} = -8.281$$

For **criterion of DANG VAN-PAPADOPOULOS**, the value of the ray of the smallest sphere circumscribed with the loading, the value of the maximum hydrostatic pressure and the value of the criterion are tested:

$$K^* = 313.579 \text{ Mpa} \quad P_{max} = 137. \text{ Mpa} \quad R_{crit} = -8.281$$

### 2.2 Modelings B, C, D, E, F and G

One bases oneself on the modelings calculated by `CALC_FATIGUE` in CAS-test SSLV135. See [V3.04.135] for the reference solutions.

### 2.3 Uncertainty on the solution

Solutions analytical or obtained from `CALC_FATIGUE`.

### 2.4 Bibliographical references

1. Thesis of I. PAPADOPOULOS "Tires polycyclic metals: a new approach" (1987) ENPC.

## 3 Modeling A

### 3.1 Characteristics of modeling

The criteria are tested CROSSLAND , DANG VAN-PAPADOPOULOS and in formula.

### 3.2 Characteristics of the grid

The grid is not necessary.

### 3.3 Sizes tested and results

For criteria called by the names:

Identification	Type of reference	Value of reference
<b>Criterion of CROSSLAND</b>		
PRES_HYDRO_MAX ( $P_{max}$ )	' SOURCE_EXTERNE '	137.
AMPLI_CISSION ( $\tau_a$ )	' SOURCE_EXTERNE '	313,579
Criterion ( $R_{crit}$ )	' SOURCE_EXTERNE '	- 8,281
<b>Criterion of DANG VAN-PAPADOPOULOS</b>		
PRES_HYDRO_MAX ( $P_{max}$ )	' SOURCE_EXTERNE '	137.
RAYON_SPHERE ( $k^*$ )	' SOURCE_EXTERNE '	313,579
Criterion ( $R_{crit}$ )	' SOURCE_EXTERNE '	- 8,281

For criteria called by the formula:

Identification	Type of reference	Value of reference
<b>Criterion of CROSSLAND</b>		
PHYDRM ( $P_{max}$ )	' SOURCE_EXTERNE '	137.
AMPCIS ( $\tau_a$ )	' SOURCE_EXTERNE '	313,579
Criterion ( $R_{crit}$ )	' SOURCE_EXTERNE '	- 8,281
<b>Criterion of DANG VAN-PAPADOPOULOS</b>		
PHYDRM ( $P_{max}$ )	' SOURCE_EXTERNE '	137.
RAYSPH ( $k^*$ )	' SOURCE_EXTERNE '	313,579
Criterion ( $R_{crit}$ )	' SOURCE_EXTERNE '	- 8,281

## 4 Modeling B

### 4.1 Characteristics of modeling

One tests the criteria in formulas (to find the results of CAS-test SSLV135D), 'MATAKE\_MODI\_AC' DANG\_VAN\_MODI\_AC (to find the results of CAS-tests SSLV135With) ;

### 4.2 Characteristics of the grid

The grid is not necessary.

### 4.3 Sizes tested and results

For the sizes of SSLV135D:

Identification	Type of reference	Value of reference
'DEPSPE'	'ANALYTICAL'	7.5E-4
'EPSPR1'	'ANALYTICAL'	7.625E-4
'SIGNM1'	'ANALYTICAL'	200
'APHYDR'	'ANALYTICAL'	66.6666
'DENDIS'	'ANALYTICAL'	0.45
'DENDIE'	'ANALYTICAL'	0.173333
'DSIGE0'	'ANALYTICAL'	200
'EPSNM1'	'ANALYTICAL'	1.75E-3
'INVA2S'	'ANALYTICAL'	1.616666E-3
'DSITRE'	'ANALYTICAL'	50
'DEPTRE'	'ANALYTICAL'	6.0625E-4
'DEPTRE'	'ANALYTICAL'	3.67423E-3
'DEPSEE'	'ANALYTICAL'	0.000866666666

For the criteria 'MATAKE\_MODI\_AC' and the criterion in formula associated (SSLV135A) with the option COURBE\_GRD\_VIE = 'WOHLER' and for the option COURBE\_GRD\_VIE = 'FORMES\_VIE' and FORMULE\_VIE = WHOL:

Identification	Type of reference	Value of reference
$\Delta \tau(n_1)$	'ANALYTICAL'	1.500000E+02
component $x$ of $n_1$	'ANALYTICAL'	-7.071068E-01
component $y$ of $n_1$	'ANALYTICAL'	7.071068E-01
component $z$ of $n_1$	'ANALYTICAL'	0.0
$N_{\max}(n_1)$	'ANALYTICAL'	5.000000E+01
$N_m(n_1)$	'ANALYTICAL'	0.0

$\varepsilon_{\max}(n_1)$	'ANALYTICAL'	1.750000E-04
$\varepsilon_m(n_1)$	'ANALYTICAL'	0.0
$\sigma_{eq}(n_1)$	'ANALYTICAL'	3.000000E+02
$Nb_{cr}(n_1)$	'ANALYTICAL'	1.094600E+04
$ENDO(n_1)$	'ANALYTICAL'	9.135647E-05
$\Delta \tau(n_2)$	'ANALYTICAL'	1 . 500000E+02
component $x$ of $n_2$	'ANALYTICAL'	7.071068E-01
component $y$ of $n_2$	'ANALYTICAL'	7.071068E-01
component $z$ of $n_2$	'ANALYTICAL'	0.0
$N_{\max}(n_2)$	'ANALYTICAL'	5.000000E+01
$N_m(n_2)$	'ANALYTICAL'	0.0
$\varepsilon_{\max}(n_2)$	'ANALYTICAL'	1.750000E-04
$\varepsilon_m(n_2)$	'ANALYTICAL'	0.0
$\sigma_{eq}(n_2)$	'ANALYTICAL'	3.000000E+02
$Nb_{cr}(n_2)$	'ANALYTICAL'	1.094600E+04
$ENDO(n_2)$	'ANALYTICAL'	9.135647E-05

For the criteria 'DANG\_VAN\_MODI\_AC' and the associated criterion in formula (SSLV135With) with the option COURBE\_GRD\_VIE = 'WOHLER' and for the option COURBE\_GRD\_VIE = 'FORMES\_VIE' and FORMULE\_VIE = 'WHOL' :

Identification	Type of reference	Value of reference
$\Delta \tau(n_1)$	'ANALYTICAL'	1 . 500000E+02
component $x$ of $n_1$	'ANALYTICAL'	7.071068E-01
component $y$ of $n_1$	'ANALYTICAL'	7.071068E-01
component $z$ of $n_1$	'ANALYTICAL'	0.0
$N_{\max}(n_1)$	'ANALYTICAL'	5.000000E+01
$N_m(n_1)$	'ANALYTICAL'	0.0
$\varepsilon_{\max}(n_1)$	'ANALYTICAL'	1.750000E-04
$\varepsilon_m(n_1)$	'ANALYTICAL'	0.0
$\sigma_{eq}(n_1)$	'ANALYTICAL'	2.750000E+02

$Nb_{cr}(n_1)$	'ANALYTICAL'	1.490300E+04
$ENDO(n_1)$	'ANALYTICAL'	6.709959E-05
$\Delta\tau(n_2)$	'ANALYTICAL'	1.500000E+02
component $x$ of $n_2$	'ANALYTICAL'	-7.071068E-01
component $y$ of $n_2$	'ANALYTICAL'	7.071068E-01
component $z$ of $n_2$	'ANALYTICAL'	0.0
$N_{max}(n_2)$	'ANALYTICAL'	5.000000E+01
$N_m(n_2)$	'ANALYTICAL'	0.0
$\varepsilon_{max}(n_2)$	'ANALYTICAL'	1.750000E-04
$\varepsilon_m(n_2)$	'ANALYTICAL'	0.0
$\sigma_{eq}(n_2)$	'ANALYTICAL'	2.750000E+02
$Nb_{cr}(n_2)$	'ANALYTICAL'	1.490300E+04
$ENDO(n_2)$	'ANALYTICAL'	6.709959E-05



## 5 Modeling C

### 5.1 Characteristics of modeling

They are tested criteria in formulas (to find the results of CAS-test SSLV135E)

### 5.2 Characteristics of the grid

The grid is not necessary.

### 5.3 Sizes tested and results

The value of reference corresponds to the endommagementT (ENDO1) and the results were got via **formula of Basquin** :

Identification	Type of reference	Value of reference
<b>Criteria</b>		
$\frac{ SIPR1 - SIPR2 }{2}$	'ANALYTICAL'	1.0707149E-03
$\frac{ SITN1 - SITN2 }{2}$	'ANALYTICAL'	1.0707149E-03
$\frac{SIPN1 - SIPN2}{2}$	'ANALYTICAL'	1.0707149E-03
$\frac{SIGEQ1 - SIGEQ2}{2}$	'ANALYTICAL'	4.287285E-03

The value of reference always corresponds to the damage (ENDO1) and the results were got with one **interpolation** curve of Wöhler :

Identification	Type of reference	Value of reference
<b>Criteria</b>		
$\frac{ SIPR1 - SIPR2 }{2}$	'ANALYTICAL'	1.9212572E-03
$\frac{ SITN1 - SITN2 }{2}$	'ANALYTICAL'	1.9212572E-03
$\frac{SIPN1 - SIPN2}{2}$	'ANALYTICAL'	1.9212572E-03
$\frac{SIGEQ1 - SIGEQ2}{2}$	'ANALYTICAL'	5.8175699E-03

## 6 Modeling D

### 6.1 Characteristics of modeling

They are tested criteria in formulas (to find the results of CAS-test sslv135F)

### 6.2 Characteristics of the grid

The grid is not necessary.

### 6.3 Sizes tested and results

Result got with the first loading ( SOL\_NL SSLV135F ):

The value of reference corresponds to the damage (ENDO1) and the results were got via **formula of Basquin** :

Identification	Type of reference	Value of reference
<b>Criteria</b>		
$\frac{ EPSN1 - EPSN2 }{2}$	'ANALYTICAL'	1.08363973E-05
$\frac{ ETPR1 - ETPR2 }{2}$	'ANALYTICAL'	1.0 8363973 E-0 5
$\frac{ ETEQ1 - ETEQ2 }{2}$	'ANALYTICAL'	1.06338423E-05

The value of reference always corresponds to the damage (ENDO1) and the results were got with one **interpolation** curve of Wöhler :

Identification	Type of reference	Value of reference
<b>Criteria</b>		
$\frac{ EPSN1 - EPSN2 }{2}$	'ANALYTICAL'	3.26558686E-05
$\frac{ ETPR1 - ETPR2 }{2}$	'ANALYTICAL'	3.26558686E-05
$\frac{ ETEQ1 - ETEQ2 }{2}$	'ANALYTICAL'	3.21404432E-05

Result got with the second loading ( SOL\_NL2 SSLV135F ):

The value of reference corresponds to the damage (ENDO1) and the results were got via **formula of Basquin** :

Identification	Type of reference	Value of reference
<b>Criteria</b>		
$\frac{ EPSN1 - EPSN2 }{2}$	'ANALYTICAL'	1.449229E-04

$\frac{ ETPR1 - ETPR2 }{2}$	'ANALYTICAL'	1. 449229 E-0 4
$\frac{ ETEQ1 - ETEQ2 }{2}$	'ANALYTICAL'	6.5320499E-05

The value of reference always corresponds to the damage (ENDO1) and the results were got with one **interpolation** curve of Wöhler :

Identification	Type of reference	Value of reference
<b>Criteria</b>		
$\frac{ EPSN1 - EPSN2 }{2}$	'ANALYTICAL'	2.408735E-04
$\frac{ ETPR1 - ETPR2 }{2}$	'ANALYTICAL'	2.408735 E-0 4

Result got with the third loading ( sol\_NL3 SSLV135F ):

The value of reference corresponds to the damage (ENDO1) and the results were got via **formula of Basquin** :

Identification	Type of reference	Value of reference
<b>Criteria</b>		
$\frac{ EPPR1 - EPPR2 }{2}$	'ANALYTICAL'	1.377855E-02

The value of reference always corresponds to the damage (ENDO1) and the results were got with one **interpolation** curve of Wöhler :

Identification	Type of reference	Value of reference
<b>Criteria</b>		
$\frac{ EPPR1 - EPPR2 }{2}$	'ANALYTICAL'	2.1858445E-03

## 7 Modeling E

### 7.1 Characteristics of modeling

They are tested criteria in formulas, 'MATAKE\_MODI\_AV', 'DANG\_VAN\_MODI\_AV', 'FATESOCI\_MODI\_AV' (to find the results of CAS-tests SSLV135B)

### 7.2 Characteristics of the grid

The grid is not necessary.

### 7.3 Sizes tested and results

For the criteria 'MATAKE\_MODI\_AV' and the associated criterion in formula ( SSLV135B )

For the results with the option COURBE\_GRD\_VIE='WOHLER' and for the option COURBE\_GRD\_VIE = 'FORMES\_VIE' and FORMULE\_VIE = 'WHOL' :

Identification	Type of reference	Value of reference
component $x$ of $n_1$ and $n_2$	'AUTRE_ASTER',	-0.38268343236509 0.38268343236509
component $y$ of $n_1$ and $n_2$	'AUTRE_ASTER',	0.92718385456679 0.92387953251129
component $z$ of $n_1$ and $n_2$	'AUTRE_ASTER',	0.00000000000000E+00
$ENDO(n_1)$	'AUTRE_ASTER',	7.0532362250863E-04

In the table above, the components  $x$  and  $y$  of  $n_1$  and  $n_2$  two values have because there exist two vectors which correspond to the same value of damage  $ENDO(n_1) = ENDO(n_2)$ .

For the results with the option COURBE\_GRD\_VIE='FORMES\_VIE' and FORMULE\_VIE = WHOL\_F:

Identification	Type of reference	Value of reference
component $x$ of $n_1$ and $n_2$	'AUTRE_ASTER',	-0.38268343236509 0.38268343236509
component $y$ of $n_1$ and $n_2$	'AUTRE_ASTER',	0.92718385456679 0.92387953251129
component $z$ of $n_1$ and $n_2$	'AUTRE_ASTER',	0.00000000000000E+00
$ENDO(n_1)$	'AUTRE_ASTER',	3.3180845213285E-04

In the table above, the components  $x$  and  $y$  of  $n_1$  and  $n_2$  two values have because there exist two vectors which correspond to the same value of damage  $ENDO(n_1) = ENDO(n_2)$ .

For the criteria 'DANG\_VAN\_MODI\_AV' and the associated criterion in formula (SSLV135B)

For the results with the option COURBE\_GRD\_VIE=' WOHLER' and for the option COURBE\_GRD\_VIE=' FORMES\_VIE' and FORMULE\_VIE = WHOL:

Identification	Type of reference	Value of reference
component $x$ of $n_1$ and $n_2$	'AUTRE_ASTER'	-7.0710678118655E-01 7.0710678118655E-01
component $y$ of $n_1$ and $n_2$	'AUTRE_ASTER'	7.0710678118655E-01
component $z$ of $n_1$ and $n_2$	'AUTRE_ASTER'	0.0000000000000E+00
$ENDO(n_1)$	'AUTRE_ASTER'	1.3419917535855E-04

In the table above, the components  $x$  and  $y$  of  $n_1$  and  $n_2$  two values have because there exist two vectors which correspond to the same value of damage  $ENDO(n_1) = ENDO(n_2)$ .

For the results with the option COURBE\_GRD\_VIE= 'FORMES\_VIE' and FORMULE\_VIE = WHOL\_F:

Identification	Type of reference	Value of reference
component $x$ of $n_1$ and $n_2$	'AUTRE_ASTER'	-7.0710678118655E-01 7.0710678118655E-01
component $y$ of $n_1$ and $n_2$	'AUTRE_ASTER'	7.0710678118655E-01
component $z$ of $n_1$ and $n_2$	'AUTRE_ASTER'	0
$ENDO(n_1)$	'AUTRE_ASTER'	8.7633062468223E-05

In the table above, the components  $x$  and  $y$  of  $n_1$  and  $n_2$  two values have because there exist two vectors which correspond to the same value of damage  $ENDO(n_1) = ENDO(n_2)$ .

For the criteria ' FATESOCI\_MODI\_AV ' and the associated criterion in formula (SSLV135B)

For the results with the option COURBE\_GRD\_VIE=' WOHLER', COURBE\_GRD\_VIE=' FORMES\_VIE' and FORMULE\_VIE = MANCO1:

Identification	Type of reference	Value of reference
component $x$ of $n_1$ and $n_2$	'AUTRE_ASTER'	-4.3837114678908E-01 4.3837114678908E-01
component $y$ of $n_1$ and $n_2$	'AUTRE_ASTER'	0.90258528434986
component $z$ of $n_1$ and $n_2$	'AUTRE_ASTER'	0
$ENDO(n_1)$	'AUTRE_ASTER'	0.43649132038876

In the table above, the component  $x$  of  $n_1$  and  $n_2$  has two values because there exist two vectors which correspond to the same value of damage  $ENDO(n_1) = ENDO(n_2)$ .

## 8 Modeling F

### 8.1 Characteristics of modeling

They are tested criteria `MATAKE_MODI_AC`, `DANG_VAN_MODI_AC`, `MATAKE_MODI_AV`, `DANG_VAN_MODI_AV`, `FATESOCI_MODI_AV`. One tests the change of the direction of the critical plan on which the damage or shearing is maximum (to find the results of CAS-tests SSLV135G )

### 8.2 Characteristics of the grid

The grid is not necessary.

### 8.3 Sizes tested and results

- Criteria of `DANG_VAN_MODI_AC`, of `MATAKE_MODI_AC`, of `DANG_VAN_MODI_AV`  
For the results of  $\phi_z$  with the node `NI` for an elastic material.

Value of $\alpha$	Type of reference	Value of reference
-1,-0.5,0..10	'ANALYTICAL'	45

For the results of  $\phi_z$  with the node `NI` for an elastoplastic material.

Value of $\alpha$	Type of reference	Value of reference
0,1,2,3,4	'ANALYTICAL'	45

- Criterion of `MATAKE_MODI_AV`

Value of $\alpha$	Type of reference	Value of reference
-1	'ANALYTICAL'	45
-0.5	'ANALYTICAL'	45,72
0	'ANALYTICAL'	46,43
0,5	'ANALYTICAL'	47,14
1	'ANALYTICAL'	47,86
1,5	'ANALYTICAL'	48,56
2	'ANALYTICAL'	49,27
2,5	'ANALYTICAL'	49,96
3	'ANALYTICAL'	50,65
3,5	'ANALYTICAL'	51,34
4	'ANALYTICAL'	52,02
4,5	'ANALYTICAL'	52,69
5	'ANALYTICAL'	53,35
5,5	'ANALYTICAL'	54
6	'ANALYTICAL'	54,65
6,5	'ANALYTICAL'	55,28

7	'ANALYTICAL'	55,9
7,5	'ANALYTICAL'	56,51
8	'ANALYTICAL'	57,11
8,5	'ANALYTICAL'	57,7
9	'ANALYTICAL'	58,28
9,5	'ANALYTICAL'	58,85
10	'ANALYTICAL'	59,41

For the results of  $\phi_z$  with the node *NI* for an elastoplastic material.

Value of $\alpha$	Type of reference	Value of reference
0	'ANALYTICAL'	46,43
1	'ANALYTICAL'	47,86
2	'ANALYTICAL'	49,27
3	'ANALYTICAL'	50,65
4	'ANALYTICAL'	52,02

- **Criterion of FATESOCI\_MODI\_AV**

For the results of  $\phi_z$  with the node *NI* for an elastic material.

Value of $\alpha$	Type of reference	Value of reference
-1	'ANALYTICAL'	45
-0,5	'ANALYTICAL'	45,34
0	'ANALYTICAL'	45,67
0,5	'ANALYTICAL'	45,99
1	'ANALYTICAL'	46,31
1,5	'ANALYTICAL'	46,61
2	'ANALYTICAL'	46,91
2,5	'ANALYTICAL'	47,2
3	'ANALYTICAL'	47,48
3,5	'ANALYTICAL'	47,75
4	'ANALYTICAL'	48,01
4,5	'ANALYTICAL'	48,27
5	'ANALYTICAL'	48,51
5,5	'ANALYTICAL'	48,75
6	'ANALYTICAL'	48,98
6,5	'ANALYTICAL'	49,2
7	'ANALYTICAL'	49,42

7,5	'ANALYTICAL'	49,63
8	'ANALYTICAL'	49,83
8,5	'ANALYTICAL'	50,03
9	'ANALYTICAL'	50,22
9,5	'ANALYTICAL'	50,4
10	'ANALYTICAL'	50,58

For the results of  $\phi_z$  with the node  $NI$  for an elastoplastic material.

Value of $\alpha$	Type of reference	Value of reference
0	'ANALYTICAL'	45,67
1	'ANALYTICAL'	46,31
2	'ANALYTICAL'	46,91
3	'ANALYTICAL'	47,48
4	'ANALYTICAL'	48,01



## 9 Modeling G

### 9.1 Characteristics of modeling

The features tested are new sizes and the keyword `FORMULE_CRITIQUE`. Only the option `CRITERE='FORMULE_CRITERE'`, `MATAKE_MODI_AC` and `DANG_VAN_MODI_AC` order `POST_FATIGUE` and the curves of life called by the formulas are used.

To find the results of CAS-tests SSLV135G and SSLV135A

### 9.2 Characteristics of the grid

The grid is identical to that of modeling A.

### 9.3 Sizes tested and results

To find the results of CAS-tests SSLV135:

Identification	Type of reference	Value of reference
<b>FORMULE_CRITIQUE =</b> 'DTAUCR' or 'MTAUCR'		
'SIGEQ1'	'ANALYTICAL'	100 MPa
'ENDO1'	'ANALYTICAL'	1.028E-6
'NBRUP1'	'ANALYTICAL'	9.73E5
'VNMI1X', 'VNMI1Y', 'VNMI1Z'	'ANALYTICAL'	(0,707, -0,707), 0,707.0
<b>FORMULE_CRITIQUE =</b> 'DGAMCR' or 'MGAMCR'		
'SIGEQ1'	'ANALYTICAL'	9.73E5
'ENDO1'	'ANALYTICAL'	1.583E-4
'NBRUP1'	'ANALYTICAL'	6.3163E3
'VNMI1X', 'VNMI1Y', 'VNMI1Z'	'ANALYTICAL'	(0,707, -0,707), 0,707.0
<b>FORMULE_CRITIQUE =</b> 'DSINCR' or 'MSINCR'		
'SIGEQ1'	'ANALYTICAL'	200
'ENDO1'	'ANALYTICAL'	1.348E-5
'NBRUP1'	'ANALYTICAL'	7.418E4
'VNMI1X', 'VNMI1Y', 'VNMI1Z'	'ANALYTICAL'	(- 1.1), 0.0174,0
<b>FORMULE_CRITIQUE =</b> 'DEPNCR' or 'MEPNCR'		
'SIGEQ1'	'ANALYTICAL'	1.75E-3
'ENDO1'	'ANALYTICAL'	2.11E-5

'NBRUP1'	'ANALYTICAL'	4.74E4
'VNM1X', 'VNM1Y', 'VNM1Z'	'ANALYTICAL'	(- 1, 1), 0.0174,0
<b>FORMULE_CRITIQUE =</b> 'DGAMPC' or 'MGAMPC'		
'SIGEQ1'	'ANALYTICAL'	1.125E-3
'ENDO1'	'ANALYTICAL'	1.3782E-6
'NBRUP1'	'ANALYTICAL'	7.256E5
'VNM1X', 'VNM1Y', 'VNM1Z'	'ANALYTICAL'	(0,707, -0,707), 0,707.0
<b>FORMULE_CRITIQUE =</b> 'DEPNPC' or 'MEPNPC'		
'SIGEQ1'	'ANALYTICAL'	0.75E-3
'ENDO1'	'ANALYTICAL'	1.126E-7
'NBRUP1'	'ANALYTICAL'	8.88E6
'VNM1X', 'VNM1Y', 'VNM1Z'	'ANALYTICAL'	(- 1.1), 0.0174,0

To find the results of CAS-tests SSLV135A:

Identification	Type of reference	Value of reference
<b>CRITERION = MATAKE_MODI_AC</b> <b>FORMULE_CRITIQUE =</b> 'DTAUCR'		
'DTAUCR'	'ANALYTICAL'	1.50E+02 MPa
'MSINCR'	'ANALYTICAL'	5.00000000000000E+01
'VNM1X' 'VNM1Y' 'VNM1Z'	'ANALYTICAL'	7.0710678118655E-01 7.0710678118655E-01 0
<b>CRITERION =</b> <b>DANG_VAN_MODI_AC</b> <b>FORMULE_CRITIQUE =</b> 'DTAUCR'		
'DTAUCR'	'ANALYTICAL'	1.50E+02 MPa
'PHYDRM'	'ANALYTICAL'	33.3333333333333
'VNM1X' 'VNM1Y' 'VNM1Z'	'ANALYTICAL'	7.0710678118655E-01, 7.0710678118655E-01, 0

## 10 Summary of the results

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Results provided by *Code\_Aster* with `POST_FATIGUE` coincide perfectly with those and values of reference obtained with `CALC_FATIGUE`.