

## SSNL137 - Draw bars in elastoplasticity with the method IMPLEX

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### Summary:

This test allows a simple checking of calculations with the law `VMIS_ISOT_LINE` for the elements of bar.

One considers an elastoplastic bar in simple traction. The resolution is carried out with the method `IMPLEX`. The tests are carried out on the constraints and the deformations and are compared with the analytical solution.

## 1 Problem of reference

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### 1.1 Geometry

A bar of  $1\text{cm}$  of length, cut out in 4 elements of  $2,5\text{mm}$ . It is embedded at an end and undergoes an imposed displacement  $U$  with the other.

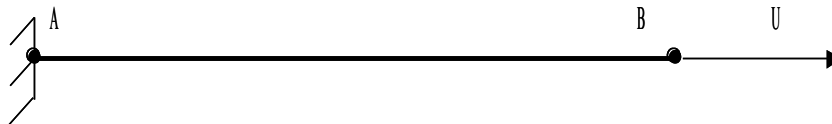


Illustration 1 : Diagram of the geometry of the bar in traction

The surface of the cross sections is worth  $A=1\text{m}^2$ .

### 1.2 Material properties

One considers an elastoplastic material with linear isotropic work hardening (VMIS\_ISOT\_LINE) with the following characteristics:

$$E=100\,000\text{MPa}$$

$$\nu=0,3$$

$$E_T=10000\text{MPa}$$

$$\sigma_Y=100\text{MPa}$$

### 1.3 Boundary conditions and loadings

Embedding in  $A$  ( $DZ=DY=DX=0$ ).

In order to avoid the movements of rigid body,  $DZ=DY=0$  for all the nodes.

Only one loading is applied: a traction in displacement imposed of  $U=1\text{mm}$  with the node  $B$ .

## 2 Reference solution

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### 2.1 Method of calculating used for the reference solution

Traction simple armature of the uniform fields of constraints and deformation. By definition, one a:

$$\sigma = \sigma_Y + E_T \left( \frac{U}{L} - \frac{\sigma}{E} \right) = 190\text{MPa}$$
$$\varepsilon = \frac{U}{L} = 0,01$$

### 2.2 Results of reference

- Constraint with the node  $B$  :  $\sigma_B=190\text{MPa}$
- Deformation with the node  $B$  :  $\varepsilon_B=0,01$

### 2.3 Uncertainty on the solution

Analytical solution. However, with the method IMPLEX who is an approached method, a small error is possible. One admits a tolerance of  $0,1\%$ .

## 3 Modeling A

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### 3.1 Characteristics of modeling

The bar is modelled by elements of bar.

### 3.2 Characteristics of the grid

Four meshes SEG2.

### 3.3 Sizes tested and results

The sizes tested are indexed in the table below.

Size tested	Type of reference	Value of reference	Allowed tolerance
$\sigma_B$	Analytical	190 MPa	0,10%
$\varepsilon_B$	Analytical	0,01	0,10%

Table 3.1 : Results of modeling A

## 4 Summary of the results

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The results being exact, it is deduced that the method `IMPLEX` is correctly programmed for the elements of bar with the relation `VMIS_ISOT_LINE`.