

SSLV116 – Circular crack in medium 3D with initial constraints.

Summary:

The purpose of this test is to validate the calculation of the stress intensity factors (SIFs) along the bottom of a crack 3D, within the framework of elasticity in the presence of initial constraints.

This test model a cube embedded on all its faces, presenting a plane central circular crack. It is subjected to an initial stress field due to the application of a thermal field.

This test contains 2 modelings:

- Modeling a: the crack is with a grid (FEM);
- Modeling B (presentE in the file of validation): the crack is not with a grid, it is represented by level-sets (X-FEM).

For two modelings, the stress intensity factors are evaluated by the orders `POST_K1_K2_K3` and `CALC_G`.

The digital values are compared with the values obtained in the case of the thermal loading are equivalent.

1 Problem of reference

1.1 Geometry

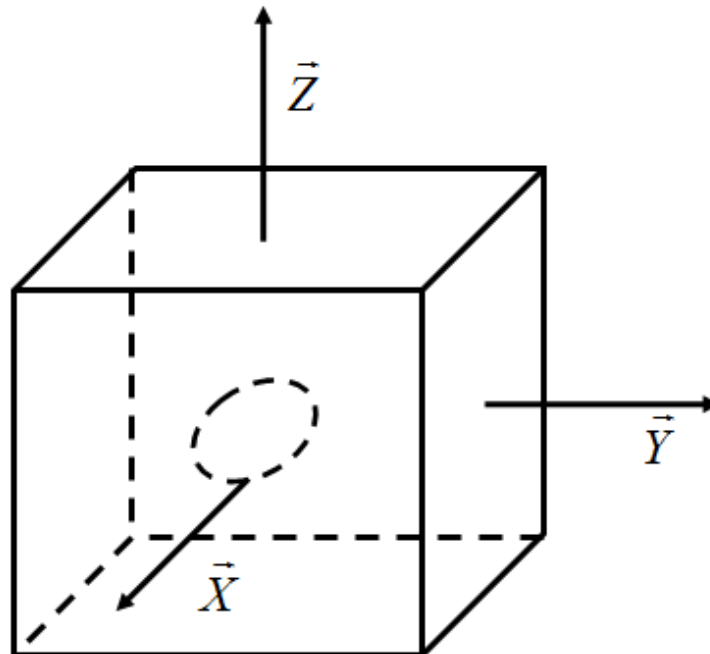


Figure 1.1 - Geometry of the case test.

The crack is to circularE (penny shaped ace) of ray $a=2m$ in the plan OXY . The with dimensions one of the cube is length $L=10a$. Thus, it is considered that the crack is in an infinite medium.

1.2 Material properties

The material, isotropic rubber band, have the properties:

$$E = 200000 \text{ MPa}$$

$$\nu = 0,3$$

$$\alpha = 0,00001 \text{ K}^{-1}$$

1.3 Boundary conditions and loadings

The outsides of volume are embedded.

Taking into account symmetries, one models only the moitié of the structure, namely it half space such as $Y > 0$. Conditions of symmetry are thus applied to the face $Y=0$: on this face, following displacement Y is blocked.

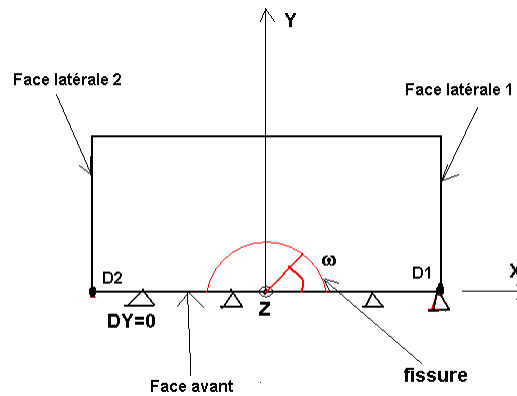


Figure 1.2: Condition of symmetry

The structure, initially of uniform temperature 250°C, is subjected to a field of variable temperature in space, according to Z. the structure cools, but is embedded of all shares. So constraints of opening are created on the crack.

The Figure below presents the profile of temperature imposed.

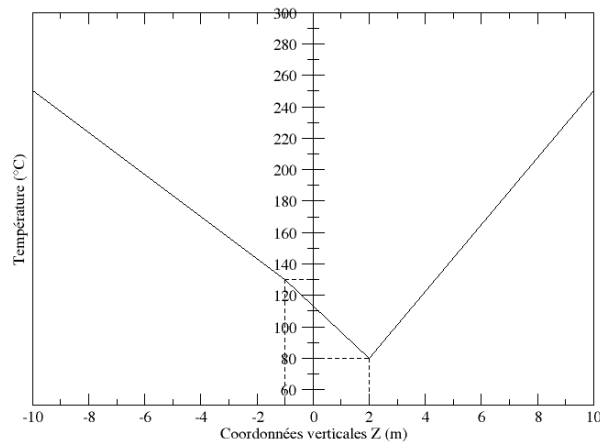


Figure 1.3 - Field of temperature imposed.

L'application of this field of temperature generate constraints (closed crack). These constraints are then extracted and constitute an initial stress field for the calculation of the factors of intensity of the constraints.

2 Reference solution

The reference solution is determined by calculation of the factors of intensity of the constraints directly starting from the thermal loading.

The validation is made starting from the maximum of the rate of refund of energy room (in each node of the face of crack) and of the factor of intensity of the constraints room to 90° of the crack.

3 Modeling A

3.1 Characteristics of modeling

In this modeling, the crack is with a grid (case FEM). The grid comprises a torus surrounding the bottom of crack.

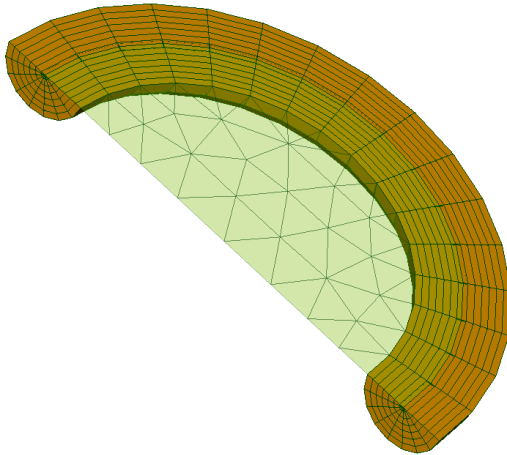


Figure 3.1: radiant grid

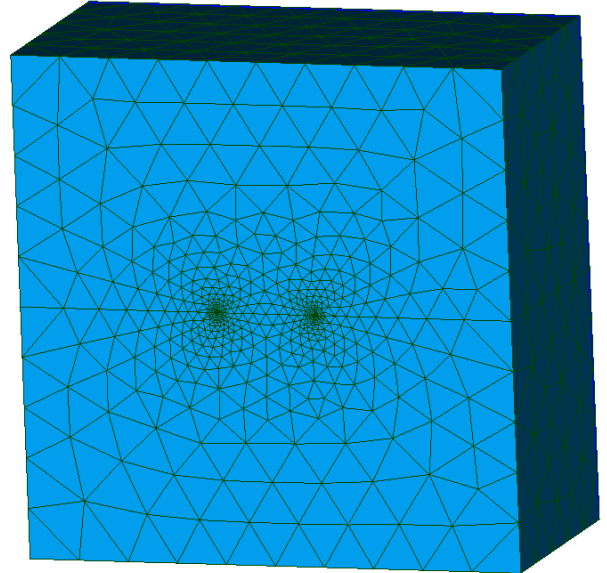


Figure 3.2: grid of the structure

3.2 Characteristics of the grid

Many nodes: 26673

Number of meshes and type: 16 SEG3, 1540 TRIA6, 416 QUAD8, 12818 TETRA10, 256 PENTA15, 256 PYRAM13, and 1536 HEXA20.

On the level of the torus (figure 3.1), the length of the prisms in the radial direction is of $h_{pris} = 0,04 m$ (layer of PENTA15 connected to the bottom of crack), and the length of the hexahedrons in the radial direction is of $h_{hexa} = 0,06 m$ (6 layers D'elements HEXA20).

The nodes mediums of the edges of meshes concerning the bottom of crack (PENTA15) are moved with the quarter of these edges (elements of Barsoum).

3.3 Results

Three crowns of integration of the field theta for the order CALC_G are used:

- Crown 1: $RINF = h_{pris} + 0,25 h_{hexa}$ and $RSUP = h_{pris} + 3,25 h_{hexa}$;
- Crown 2: $RINF_2 = h_{pris} + 0,25 h_{hexa}$ and $RSUP_2 = h_{pris} + 5,25 h_{hexa}$;
- Crown 3: $RINF_3 = h_{pris} + 2,25 h_{hexa}$ and $RSUP_3 = h_{pris} + 5,25 h_{hexa}$.

A smoothing of the type is chosen LEGENDRE.

The parameter ABS_CURV_MAXI of the operator POST_K1_K2_K3 is selected so as to retain 5 nodes on the segment of extrapolation.

K_j is tested only at the point such as $(\theta) = 90^\circ$ (see figure 1.2).

3.4 Sizes tested

Warning : The translation process used on this website is a "Machine Translation". It may be imprecise and inaccurate in whole or in part and is provided as a convenience.

Copyright 2019 EDF R&D - Licensed under the terms of the GNU FDL (<http://www.gnu.org/copyleft/fdl.html>)

One tests many sizes here, in order to control the thermal reference and the initial state.

Identificatio n	Option of calculation	Notice	Type of reference	Value of reference	% Toleranc e
$max(Gref)$	CALC_G, thermics	Couronne1	'NOT REGRESSION'	1923355.09151	1.E-4 %
$max(Gref\ 2)$	CALC_G, thermics	Couronne2	'ANOTHER ASTER'	1923355.09151	2.E-2 %
$max(Gref\ 3)$	CALC_G, thermics	Couronne3	'ANOTHER ASTER'	1923355.09151	4.E-2 %
$max(Girref)$	CALC_K_G, thermics	Couronne1	'ANOTHER ASTER'	1923355.09151	1.E-4 %
$max(Gini)$	CALC_G, initial constraint	Couronne1 initial constraint Gauss	'ANOTHER ASTER'	1923355.09151	2.E-2 %
$max(Gini2)$	CALC_G, initial constraint	Couronne2 initial constraint Gauss	'ANOTHER ASTER'	1923355.09151	7.E-3 %
$max(Gini3)$	CALC_G, initial constraint	Couronne3 initial constraint Gauss	'ANOTHER ASTER'	1923355.09151	1.E-3 %
$max(Gini4)$	CALC_G, initial constraint	Couronne1 initial constraint Node	'ANOTHER ASTER'	1923355.09151	2.E-2 %
$max(Gini5)$	CALC_G, initial constraint	Couronne2 initial constraint Node	'ANOTHER ASTER'	1923355.09151	7.E-3 %
$max(Gini6)$	CALC_G, initial constraint	Couronne3 initial constraint Node	'ANOTHER ASTER'	1923355.09151	1.E-3 %
$max(Girini)$	CALC_K_G, initial constraint	Couronne1 initial constraint Gauss	'ANOTHER ASTER'	1923355.09151	2.E-2 %
$max(Girini2)$	CALC_K_G, initial constraint	Couronne2 initial constraint Gauss	'ANOTHER ASTER'	1923355.09151	9.E-3 %
$max(Girini3)$	CALC_K_G, initial constraint	Couronne3 initial constraint Gauss	'ANOTHER ASTER'	1923355.09151	5.E-3 %
$max(Girini4)$	CALC_K_G, initial constraint	Couronne1 initial constraint Node	'ANOTHER ASTER'	1923355.09151	2.E-2 %
$max(Girini5)$	CALC_K_G, initial constraint	Couronne2 initial constraint Node	'ANOTHER ASTER'	1923355.09151	9.E-3 %
$max(Girini6)$	CALC_K_G, initial constraint	Couronne3 initial constraint Node	'ANOTHER ASTER'	1923355.09151	5.E-3 %

	initial constraint	initial constraint Node	ASTER'		
<i>Kref</i> (90°)	POST_K1_K2_ K3		'NOT REGRESSION'	621498251.587	5 %
Thermics					
<i>Kini</i> (90°)	POST_K1_K2_ K3		'ANOTHER ASTER'	621498251.587	1.E-4 %
Initial constraint					
<i>Girini</i> <i>K_I</i> (90°)	CALC_K_G, Initial constraint	Couronne1, initial constraint Gauss	'ANOTHER ASTER'	621498251.587	7 %
<i>Girini2</i> <i>K_I</i> (90°)	CALC_K_G, Initial constraint	Couronne2 initial constraint Gauss	'ANOTHER ASTER'	621498251.587	8 %
<i>Girini3</i> <i>K_I</i> (90°)	CALC_K_G, Initial constraint	Couronne3 initial constraint Gauss	'ANOTHER ASTER'	621498251.587	9 %
<i>Girini4</i> <i>K_I</i> (90°)	CALC_K_G, Initial constraint	Couronne1 initial constraint Node	'ANOTHER ASTER'	621498251.587	7 %
<i>Girini5</i> <i>K_I</i> (90°)	CALC_K_G, Initial constraint	Couronne2 initial constraint Node	'ANOTHER ASTER'	621498251.587	8 %
<i>Girini6</i> <i>K_I</i> (90°)	CALC_K_G, Initial constraint	Crown3 initial constraint Node	'ANOTHER ASTER'	621498251.587	9 %

4 Modeling B

4.1 Characteristics of modeling

In this modeling, the crack is not with a grid (case X-FEM).

One uses same Mayllage that for the case test sslv154b.

In order to obtain the bestE precision on the results, the free initial grid was refined on the level of the bottom of crack using the order `MACR_ADAP_MAIL`.

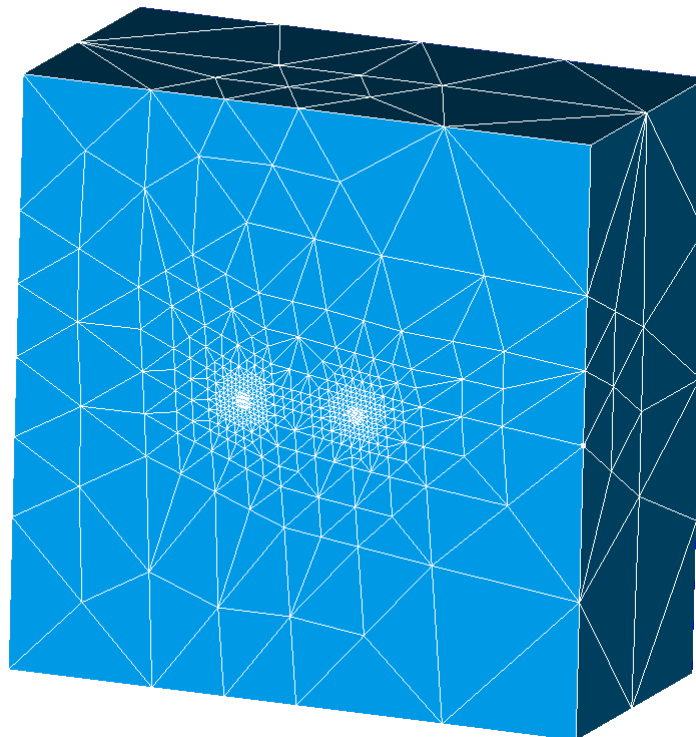


Figure 4.1: refined grid of the structure

4.2 Characteristics of the grid

Many nodes: 1146

Number of meshes and type: 64573 TETRA4

The length characteristic of an element close to the bottom to crack is of $0,07 m$.

4.3 Results

Three crowns of integration of the field theta for the order `CALC_G` are used:

- Crown 1: $RINF=0,12 m$ and $RSUP=0,528 m$.
- Crown 2: $RINF_2=0,5 RINF$ and $RSUP_2=0,5 RSUP$
- Crown 3: $RINF_2=1,5 RINF$ and $RSUP_2=1,5 RSUP$

A smoothing of the type is chosen `LEGENBRE`.

Warning : The translation process used on this website is a "Machine Translation". It may be imprecise and inaccurate in whole or in part and is provided as a convenience.

Copyright 2019 EDF R&D - Licensed under the terms of the GNU FDL (<http://www.gnu.org/copyleft/fdl.html>)

The parameter `ABS_CURV_MAXI` of the operator `POST_K1_K2_K3` is selected so as to retain 5 nodes on the segment of extrapolation.

K_I is tested only at the point such as $\omega = 90^\circ$.

Option of calculation	Case considered	Crown	Max G (J/m ²)	K1 (90°) (MPa.m ^{1/2})
POST_K1_K2_K3	Thermics			639, E6
	Initial constraint			612E6
CALC_G	Thermics		2,06E6	
	Initial constraint	1	2,03E6	
		2	1,95E6	
		3	2,06E6	
CALC_K_G	Initial constraint	1	1,92E6	677E6
		2	1,94E6	661E6
		3	2,07E6	688E6

Table 1- Results of modeling FEM.

- It is noted whereas the results are:
- In conformity with the references to 6% for G and 8% for K1. Let us note that the reference `POST_K1_K2_K3` present a variation of 4% between the thermal case and the case with initial constraints
- Different from 5% maximum for G enters the options `CALC_G` and `CALC_K_G`,
- Independent of the crown with 5% near for G of `CALC_G`, 7% for G of `CALC_K_G` and 4% for K1.

4.4 Sizes tested

As for modeling A, one tests the value maximale rates of refund of energy and the factor of intensity of the constraints for an angle of 90°, 3 crowns, in the calculation cases thermal and initial state.

However, in X-FEM, the constraints can be given only to the nodes, which limits the number of tests.

One tests many sizes, in order to control the thermal reference and the initial state.

Identificatio n	Option of calculation	Notice	Type of reference	Value of reference	% Toler ance
$max(Gref)$	CALC_G, thermics	couronne1	'NOT REGRESSION'	$2.06919 \cdot 10^6$	1%
$max(Gini)$	CALC_G, initial constraint	Couronne1	'ANOTHER ASTER'	$2.06919 \cdot 10^6$	2%
$max(Gini2)$	CALC_G, initial constraint	Couronne2	'ANOTHER ASTER'	$2.06919 \cdot 10^6$	6%
$max(Gini3)$	CALC_G, initial constraint	Couronne3	'ANOTHER ASTER'	$2.06919 \cdot 10^6$	2%
$max(Girini)$	CALC_K_G, initial constraint	Couronne1	'ANOTHER ASTER'	$2.06919 \cdot 10^6$	7 %
$max(Girini2)$	CALC_K_G, initial constraint	Couronne2	'ANOTHER ASTER'	$2.06919 \cdot 10^6$	7 %
$max(Girini3)$	CALC_K_G, initial constraint	Couronne3	'ANOTHER ASTER'	$2.06919 \cdot 10^6$	3 %
$max(Girini4)$	CALC_K_G, initial constraint	Couronne1 initial constraint Node	'ANOTHER ASTER'	$1.92013 \cdot 10^6$	1.5 %
$max(Girini5)$	CALC_K_G, initial constraint	Couronne2 initial constraint Node	'ANOTHER ASTER'	$1.95458 \cdot 10^6$	1.5 %
$max(Girini6)$	CALC_K_G, initial constraint	Couronne3 initial constraint Node	'ANOTHER ASTER'	$1.93471 \cdot 10^6$	1.5 %
$Kref(90^\circ)$	POST_K1_K2_K 3 Thermics		'NOT REGRESSION'	$6.397943 \cdot 10^8$	1 %

<i>Girini</i> $K_I(90^\circ)$	CALC_K_G, initial Constraint	Couronne1,	'ANOTHER ASTER'	6.397943 10 ⁸	7%
<i>Girini2</i> $K_I(90^\circ)$	CALC_K_G, Initial constraint	Couronne2 initial constraint Gauss	'ANOTHER ASTER'	6.397943 10 ⁸	5%
<i>Girini3</i> $K_I(90^\circ)$	CALC_K_G, initial Constraint	Couronne3 initial constraint Gauss	'ANOTHER ASTER'	6.397943 10 ⁸	8%

5 Summary of the results

This CAS-test validates the calculation of the stress intensity factors of a crack 3D in the presence of initial state.

Lmodeling by one has crack with a grid is more satisfactory than modeling X-FEM. It shows in particular one dependence less with the crown.